

A simple mathematical model for prediction of nitrogen dioxide molecular structure

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Where it is shown that one can numerically compute the angle between atomic bonds and length bonds in NO₂ molecule with a good agreement with experimental data.

In this paper we assume that nitrogen and oxygen atoms have valence electronic configuration $2s^22p^3$ and $2s^22p^4$ respectively. In NO₂ nitrogen dioxide molecule, N atom and each O atom share two pairs of electrons while N preserves a single unpaired electron (see ¹ChEBI). The pairs of electrons shared by N and O are bonding pairs, according to VSEPR theory terminology (see ^{1,2}Gillespie).

From VSEPR theory, in this molecule the three atoms have a planar configuration. Let be $\alpha = \text{ONO}$ the angle with vertex at N nucleus, that is the angle between atomic bonds. Also, we consider the circle C_N centred on N nucleus and having radius R_N equal to Van der Waals radius of N (see ¹Gillespie), and the two circles C_O centred on O nuclei and having radii R_O equal to Van der Waals radius of O, positioned along the line NO with O nucleus at a distance, from N, equal to a value d to be defined. Let be A the point of intersection between C_N and the vertical line traced from N nucleus, and B and C the two intersections between C_O and the lines NO respectively (see Fig.1). Finally, denote with χ_N and χ_O the nitrogen and oxygen electronegativities.

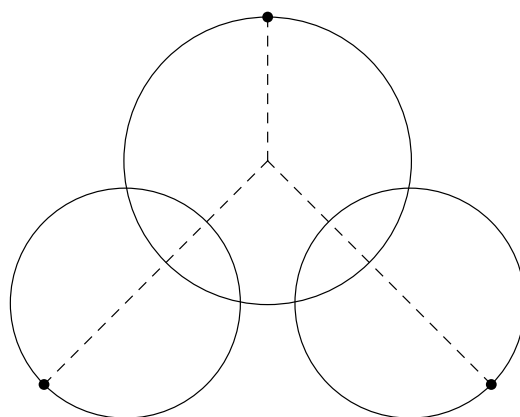


Fig. 1 *The geometrical representation of nitrogen dioxide molecule.*

In the most simple representation, assuming cr_N and cr_O the covalent radius of N and O respectively, the length d of the bonds N-O is assumed to be the sum $cr_N + cr_O$. But nitrogen and oxygen are two chemical elements having great electronegativity values, so the real length bond d is lower than the sum of the two covalent radii (see ²Gillespie). Also, $\chi_O > \chi_N$, so O atom attracts valence electrons and the extension of the bond electronic pair domain decreases along the NO direction. We can think that $d : (cr_N + cr_O) = \chi_N : \chi_O$, therefore the length bond is

$$d = (cr_N + cr_O) \frac{\chi_N}{\chi_O}$$

If Q is the charge concentration at point A of the nitrogen unpaired electron, then for the double bonds N-O the charge concentrations at points B and C, due to two valence electrons of oxygen, are $2Q$. The Coulomb electrostatic energy among the three electronic pairs domains is

$$W = Q \ 2Q \frac{1}{d_{NO}} + Q \ 2Q \frac{1}{d_{NO}} + 2Q \ 2Q \frac{1}{d_{OO}}$$

where is d_{NO} the distance between N and O atoms, and d_{OO} is the distance between O atoms in the molecule. If we consider a cartesian system with origin at the middle point of the segment BC, then the cartesian coordinates of A, B and C are $A = \{0, R_N + (d + R_O) \cos \alpha/2\}$, $B = \{-(d + R_O) \sin \alpha/2, 0\}$ and $C = \{(d + R_O) \sin \alpha/2, 0\}$ respectively. The geometric configuration of the molecule in its ground state is determined by atoms positioning so that W is minimum.

We can find numerically, using a mathematical software, the value of α for which W has its minimum (see ¹Trott). Note that, for this purpose, it is not restrictive to suppose $Q = 1$. These are the values of geometric parameters used for computation (see ¹CCCBDB and ¹Gillespie): $R_N = 150 \text{ pm}$, $R_O = 140 \text{ pm}$, $cr_N = 70 \text{ pm}$, $cr_O = 60 \text{ pm}$, $\chi_N = 3.1$, $\chi_O = 3.5$.

In Fig. 2 there is a plot of the Coulomb energy as function of the angle α the N-O bonds. Minimum is obtained for a value of 2.35 rad , that is $\alpha = 134.65^\circ$. Note that this value is in good agreement with experimental values reported in technical literature, e.i. $\alpha = 134.1^\circ$ in ¹CCCBDB.

Note that the d length bond, computed using previous formula, is 120.5 pm , to be compared with the value of 119.4 pm from experimental data (see ¹CCCBDB).

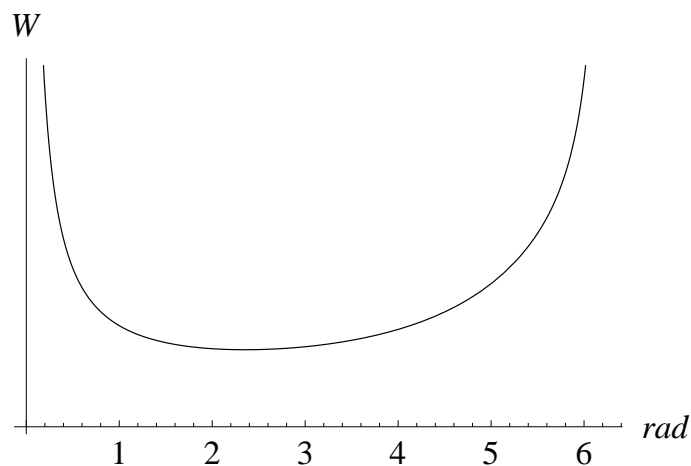


Fig. 2 Graph of the Coulomb energy vs the angle $\alpha = \text{ONO}$, due to electronic pairs in nitrogen dioxide molecule.

Summary Table

	<i>Experimental</i>	<i>This model</i>
ONO angle [°]	134.1	134.65
bond length [<i>pm</i>]	119.4	120.5

References

- ¹ CCCBDB, Computational Chemistry Comparison and Benchmark DataBase, <http://cccbdb.nist.gov/>, 2013
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